

# Detecting Fake Paintings

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Joint work with Morten Nielsen

# Outline

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## 1 Introduction

## 2 Methods

- Contourlets
- Hidden Markov Model

## 3 Results

## Problem Statement: Which is Authentic?



# Relevance

## The Art Newspaper:

### Break the silence over fakes

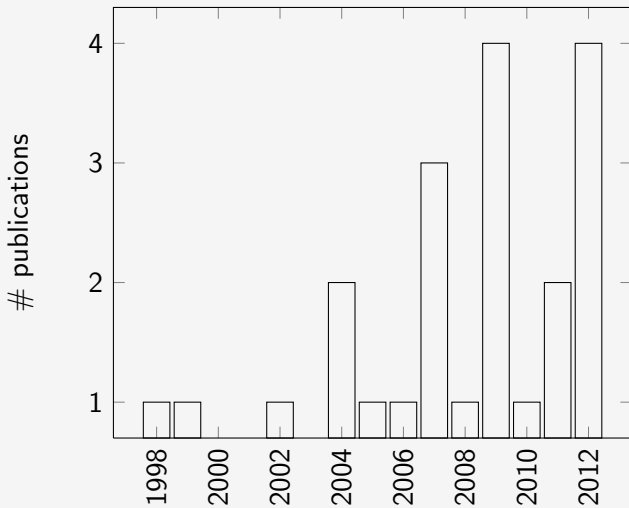
Enforced silence encourages fakes. It gives forgers the space in which they can manoeuvre

By Jack Flam. Opinion, [Issue 234, April 2012](#)

Published online: 12 April 2012

The press has recently been full of reports about forgeries. In Europe, fakes by Wolfgang Beltracchi have embarrassed a number of experts and collectors. In the US, a painting purportedly by Jackson Pollock that was sold for \$17m is the subject of a lawsuit against the now-closed Knoedler gallery and its former president Ann Freedman. This "Pollock", moreover, seems to be only the tip of the iceberg, since it appears to belong to a surprisingly large collection of pictures supposedly painted by leading abstract expressionist artists. This collection was allegedly

## Interest in this Subject



# Brushstrokes



# Brushstrokes

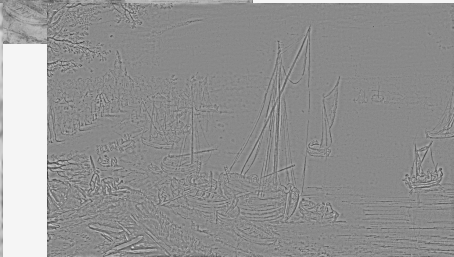


## Divide and Conquer

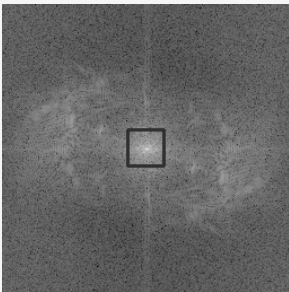




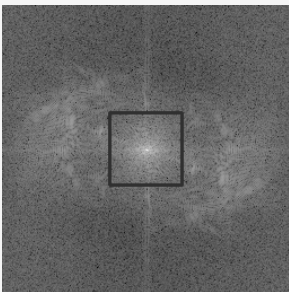
# Divide and Conquer



# Details = High Frequencies

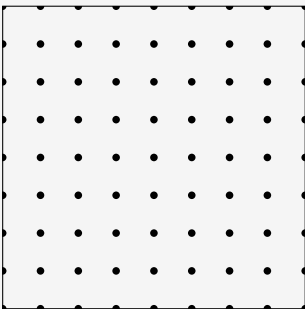


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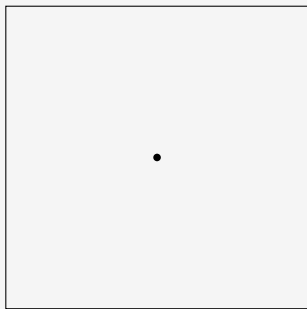


# Fourier Fails

- **Fourier: One frequency, lots of pixels**
- Heisenberg: One frequency, one pixel is impossible
- Realistic: Few frequencies, few pixels.



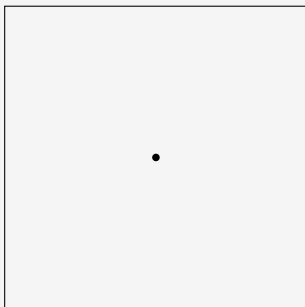
spatial



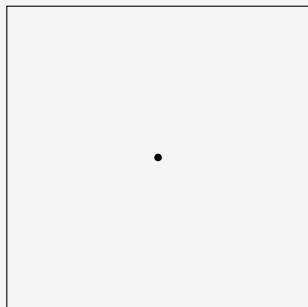
frequency

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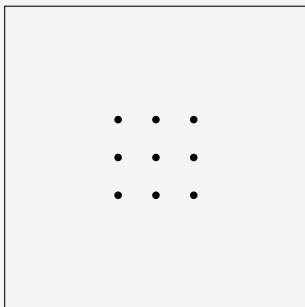
spatial



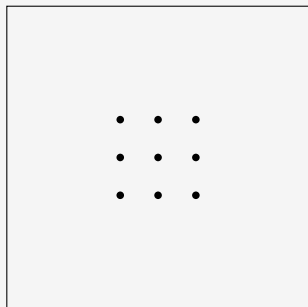
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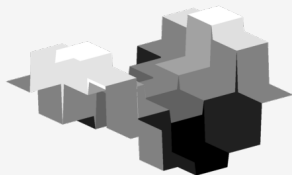
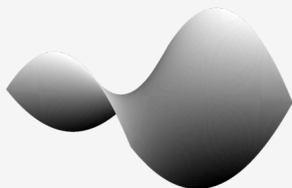
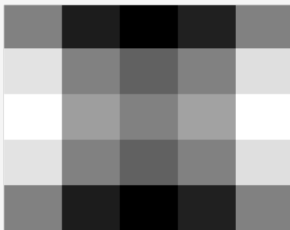
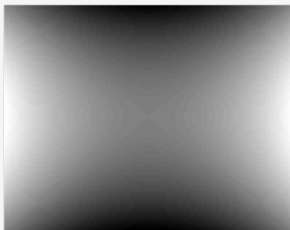
spatial



frequency

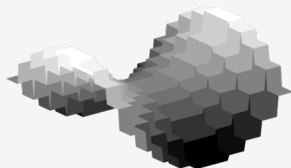
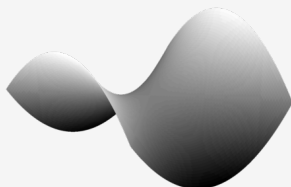
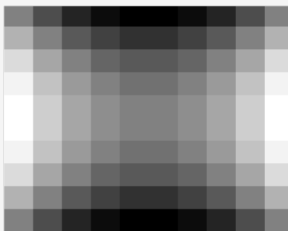
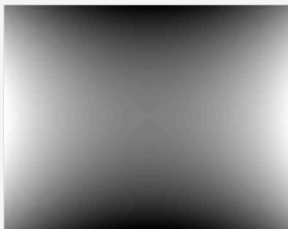
# Multiresolution Analysis: Digital image

$$\text{digital image} = \sum_{k \in \mathbb{Z}^2} a_k \phi(x - k), \quad \phi(x) = \mathbb{1}_{[0,1]^2}(x).$$



# Multiresolution Analysis: Digital image

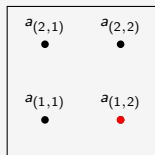
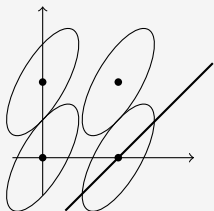
$$\text{digital image} = \sum_{k \in \mathbb{Z}^2} a_k \phi(2x - k), \quad \phi(2x) = \mathbb{1}_{[0,1/2)^2}(x).$$





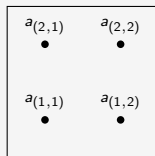
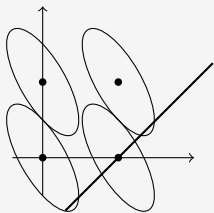
# Multiresolution Analysis: Contourlets

$$\text{digital image} = \sum_{d=0}^D \sum_{k \in \mathbb{Z}^2} a_k \psi_d(x - k).$$



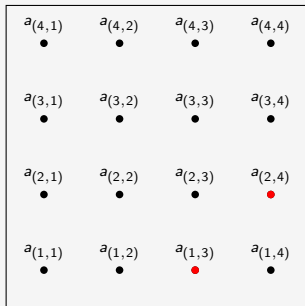
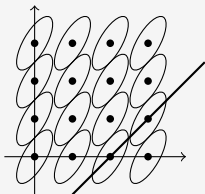
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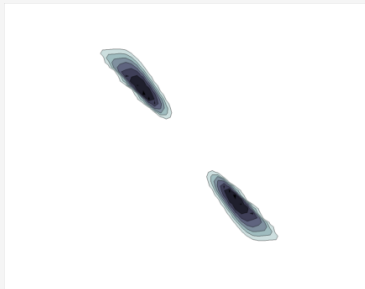
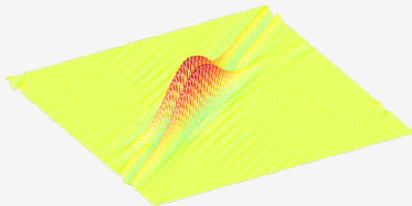
# Multiresolution Analysis: Contourlets

$$\text{digital image} = \sum_{d=0}^D \sum_{k \in \mathbb{Z}^2} a_k \psi_d(2x - k).$$



# Contourlet properties

- Directionality
- Frequency selection
- Made for digital images



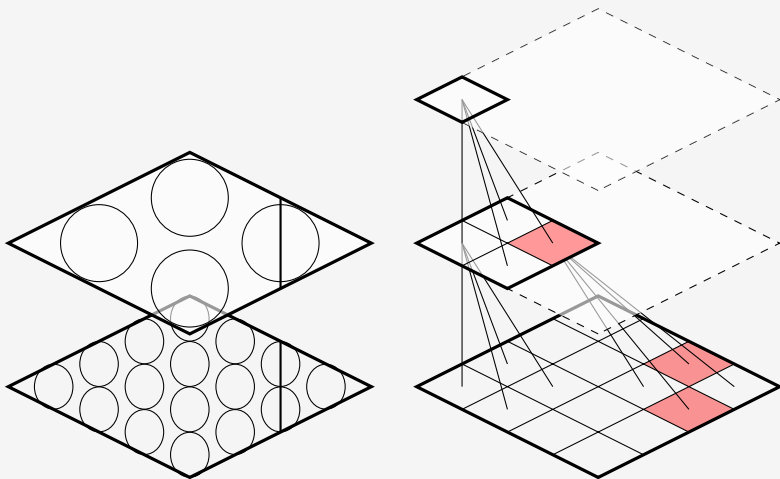
# Contourlet Transform



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# Hidden Markov Model

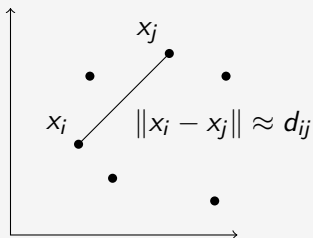


## Distances: Multidimensional Scaling

image<sub>i</sub>                  image<sub>j</sub>

↓                                  ↓

$$d(\text{HMM}_i, \text{HMM}_j) = d_{ij}$$





# Results: Pieter Bruegel the Elder



3



4



5



6



7



9



11



13



20



120



121



125

## Results: Pieter Bruegel the Elder

